TOPICAL REVIEW

Multiscale modeling and general theory of non-equilibrium plasma-assisted ignition and combustion

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Multiscale modeling and general theory of non-equilibrium plasma-assisted ignition and combustion

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Abstract
A self-consistent framework for modeling and simulations of plasma-assisted ignition and combustion is established. In this framework, a ‘frozen electric field’ modeling approach is applied to take advantage of the quasi-periodic behaviors of the electrical characteristics to avoid the re-calculation of electric field for each pulse. The correlated dynamic adaptive chemistry (CO-DAC) method is employed to accelerate the calculation of large and stiff chemical mechanisms. The time-step is dynamically updated during the simulation through a three-stage multi-time scale modeling strategy, which utilizes the large separation of time scales in nanosecond pulsed plasma discharges. A general theory of plasma-assisted ignition and combustion is then proposed. Nanosecond pulsed plasma discharges for ignition and combustion can be divided into four stages. Stage I is the discharge pulse, with time scales of O (1–10 ns). In this stage, input energy is coupled into electron impact excitation and dissociation reactions to generate charged/excited species and radicals. Stage II is the afterglow during the gap between two adjacent pulses, with time scales of O (100 ns). In this stage, quenching of excited species dissociates O2 and fuel molecules, and provides fast gas heating. Stage III is the remaining gap between pulses, with time scales of O (1–100 µs). The radicals generated during Stages I and II significantly enhance exothermic reactions in this stage. The cumulative effects of multiple pulses is seen in Stage IV, with time scales of O (1–1000 ms), which include preheated gas temperatures and a large pool of radicals and fuel fragments to trigger ignition. For flames, plasma could significantly enhance the radical generation and gas heating in the pre-heat zone, thereby enhancing the flame establishment.

Keywords: plasma fluid modeling, nanosecond plasma discharge, ignition, plasma-assisted combustion, low-temperature chemistry

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Nomenclature

\[ C_{p,k} \] specific heat at constant pressure of the \( k \)th species (\( J \cdot kg^{-1} \cdot K^{-1} \))

\[ D_k \] effective diffusion coefficient of the \( k \)th species (\( cm^2 \cdot s^{-1} \))

\[ D_e \] electron energy diffusion coefficient (\( cm^2 \cdot s^{-1} \))

\[ \text{Dec}_k \] decay rate of the \( k \)th species (\( kg \cdot cm^{-3} \cdot s^{-1} \))

\[ E \] electric field (\( V \cdot cm^{-1} \))

\[ E/N \] reduced electric field (Td)

\[ F_{t}^{\text{EHD}} \] electro-hydrodynamic force per unit volume (\( kg \cdot cm^{-2} \cdot s^{-1} \))

\[ G(t) \] non-dimensional heat transfer parameter

\[ h \] gas mixture enthalpy (\( J \cdot kg^{-1} \))

\[ h_k^{0} \] enthalpy of formation of the \( k \)th species at \( T_{ref} \) (\( J \cdot kg^{-1} \))

\[ J_e \] electron density flux (\( cm^{-2} \cdot s^{-1} \))

\[ J_{e,s} \] wall boundary flux of electrons (\( cm^{-2} \cdot s^{-1} \))

\[ J_k \] flux of the \( k \)th species (\( cm^{-2} \cdot s^{-1} \))

\[ J_e \] flux of electron energy (\( eV \cdot cm^{-2} \cdot s^{-1} \))

\[ J_{e,s} \] wall boundary flux of electron energy

\[ J_{+,-} \] net positive and negative charge fluxes, respectively (\( cm^{-2} \cdot s^{-1} \))

\[ J_{+,-,s} \] wall boundary flux of positive ions (\( cm^{-2} \cdot s^{-1} \))

\[ J_{-,s} \] wall boundary flux of negative ions (\( cm^{-2} \cdot s^{-1} \))

\[ k_d \] thermal conductivity of quartz (\( W \cdot m^{-1} \cdot K^{-1} \))

\[ k_{gw} \] thermal conductivity of the gas mixture at temperature \( T_{gw} \) (\( W \cdot m^{-1} \cdot K^{-1} \))

\[ L \] gap length (cm)

\[ l_d \] thickness of the dielectric layer (cm)

\[ M \] average molecular weight of air (kg)

\[ m_e \] electron mass (kg)

\[ N \] number density of neutral particles (\( cm^{-3} \))

\[ n_e \] outward unit normal vector

\[ n_k \] electron number density (\( cm^{-3} \))

\[ n_k^0 \] number density of the \( k \)th species (\( cm^{-3} \))

\[ n_e \] electron energy density (\( eV \cdot cm^{-3} \))

\[ n_{+,-} \] sum of number densities of positive and negative ions, respectively (\( cm^{-3} \))

\[ p \] pressure (\( kg \cdot cm^{-1} \cdot s^{-1} \))

\[ Q_e \] production rate of electron energy density (\( eV \cdot cm^{-3} \cdot s^{-1} \))

\[ \tilde{Q}_{s}^{\text{HI}} \] energy release rate from Joule heating (\( kg \cdot cm^{-1} \cdot s^{-3} \))

\[ q_{pulse} \] input energy per pulse (MJ)

\[ q_k \] energy flux from heat conduction and diffusion (\( kg \cdot s^{-1} \))

\[ q_k \] charge number of the \( k \)th species (-1 for negative ions and electrons, +1 for positive ions, and 0 for neutral species)

\[ r_i \] reaction rate of the \( i \)th electron impact reaction

\[ S_L \] laminar flame speed (\( cm \cdot s^{-1} \))

\[ S_{ign} \] ignition kernel propagation speed (\( cm \cdot s^{-1} \))

\[ T \] gas temperature (K)

\[ T_{amb} \] ambient temperature (K)

\[ T_b \] boundary temperature (K)

\[ T_e \] electron temperature (K)

\[ T_{gw} \] gas temperature at a distance \( \Delta x \) from the solid wall (K)

\[ T_{ref} \] reference temperature (K)

\[ T_{se} \] temperature of secondary electrons ejected from the electrode surface (eV)

\[ t_{pulse} \] duration of one pulse (ns)

\[ u \] convective velocity vector of the gas mixture (\( cm \cdot s^{-1} \))

\[ u_i, u_j \] flow velocity components in \( i \)th and \( j \)th directions, respectively (\( cm \cdot s^{-1} \))

\[ V_{app} \] applied voltage (V)

\[ V_{gap} \] gap voltage (V)

\[ V_{peak} \] peak value of applied voltage (kV)

\[ \gamma \] secondary electron emission coefficient for ions colliding with electrode surface

\[ \Delta E_i \] heat of the \( i \)th electron impact reaction (eV)

\[ \Delta n_{e,\text{max}} \] maximum relative difference in the electron number density at the end of two adjacent discharge pulses

\[ \epsilon \] electric permittivity (\( F \cdot cm^{-1} \))

\[ \epsilon_d \] dielectric constant

\[ \epsilon_e \] electron energy (eV)

\[ \kappa \] dynamic viscosity (\( kg \cdot cm^{-1} \cdot s^{-1} \))

\[ \lambda \] thermal conductivity of the gas mixture (\( W \cdot cm^{-2} \cdot K^{-1} \))

\[ \mu_k \] mobility of the \( k \)th species in the electric field (\( cm^2 \cdot V^{-1} \cdot s^{-1} \))

\[ \mu_e \] electron energy mobility (\( cm^2 \cdot V^{-1} \cdot s^{-1} \))

\[ \nu_{el} \] elastic collision frequency of electrons (s^{-1})

\[ \rho \] density of the plasma mixture (\( kg \cdot cm^{-3} \))
\( \tau_{ij} \) viscous shear stress tensor (kg \( \cdot \) cm\(^{-1} \) \( \cdot \) s\(^{-2} \))

\( \tau_{\text{plasma}} \) ignition delay after plasma pulse burst (s)

\( \tau_{\text{self}} \) auto-ignition delay without plasma (s)

\( \phi \) electric potential (V)

\( \dot{\omega}_k \) production term of the \( k \)th species (cm\(^{-3} \) \( \cdot \) s\(^{-1} \))

1. Introduction

Over the past decade, non-equilibrium plasma has been the subject of significant attention, due to its great potential to enhance ignition and combustion in internal combustion engines, gas turbines, scramjet engines, and pulsed detonation engines [1, 2]. Past studies have shown that nanosecond discharge plasma can shorten ignition delays [3, 4], extend the flammability limits to allow ultra-lean combustion for emission reduction [5], increase flame propagation speed [6, 7], and improve flame stabilization [8]. Despite promising results, the underlying physio-chemical processes for such enhancement are still not well understood.

The existing experimental studies can be divided into two categories. The first category attempts to study plasma-assisted combustion in complex flow environments representative of real engine combustors. For example, Zhang et al [9, 10] studied the interaction between a plasma jet and turbulent flow; Kim et al [11] investigated the effect of plasma on a fuel jet in cross flow; Starikovskaya et al [12] and Leonov et al [13, 14] examined the interaction between plasma and supersonic combustion. The complex flow structures in these experiments confounded the fundamental plasma enhancement mechanisms. In the second category, experiments are conducted in canonical configurations to simplify or even eliminate hydrodynamic effects and isolate plasma enhancement from other effects. For example, Uddi et al [15] conducted two-photon absorption laser induced fluorescence (TALIF) measurements of atomic oxygen in fuel/air mixtures subject to nanosecond pulsed discharges in a rectangular quartz reactor. Yin et al [16] studied the ignition of mildly preheated H\(_2\)/air mixtures under nanosecond pulsed discharges in a quartz flow reactor. Lefkowitz et al [17] conducted in situ measurements of nanosecond pulsed plasma activated C\(_2\)H\(_2\)/Ar pyrolysis and oxidation of C\(_2\)H\(_2\)/O\(_2\)/Ar mixtures in a flow reactor.

Although this second category of experimental studies provides more insights into the underlying physio-chemical processes of plasma enhancement, the number of measurable quantities remains limited and many conclusions are indirectly inferred. For this reason, high-fidelity modeling and simulations of plasma-assisted ignition and combustion are vital. Comprehensive numerical models of plasma have been developed over the last several decades, and the field is relatively mature. For example, Ventzek et al [18] developed a high dimensional plasma model, and Shigeta [19] reviewed a class of models for plasma-turbulence interaction. In contrast, the modeling of plasma-assisted ignition and combustion appears to be limited, primarily because the range of scales involved makes the computation extremely challenging. In addition, most of these studies [20–22] are zero-dimensional (0D), due to the complexity of plasma-combustion interaction. In 0D models, plasma discharges are assumed to be uniform over the entire domain during each pulse, and the influence of cathode sheath formation is neglected. Furthermore, because the energy input channels are difficult to model in 0D models, the reduced electric field (E/N) and electron density are pre-specified such that the coupled energy can match experimentally measured values. To address these issues, our group has developed a self-consistent, one-dimensional (1D) model [23–25] for taking into account various spatiotemporal scales involved in plasma-assisted ignition and combustion. This model resolves the transient electric field during each nanosecond discharge pulse, and calculates the cumulative effects of multiple pulses on fuel dissociation/pyrolysis, oxidation, ignition, and combustion. The work has been extensively validated in three typical configurations for a wide range of fuel types and operating conditions [26–30]. In the first half of this paper, we will summarize the different modeling strategies we have developed over the past decade.

There have been several topic reviews for the field of plasma-assisted ignition and combustion in recent years. Starikovskaya [12] and Starikovskii et al [31] summarized the discharge types, and evaluated the oxidation of different hydrocarbons by nanosecond discharge and the control of their ignition and combustion characteristics. Starikovskiy and Aleksandrov [1] reviewed the applications and physics of plasma-assisted combustion. Sun and Ju [32–34] reviewed the chemical kinetics and diagnostics of plasma-assisted low-temperature combustion. The present paper focuses on numerical modeling and attempts to develop a general multi-time scale theory of plasma-assisted ignition and combustion.

The structure of this paper is as follows. Section 2 reviews a self-consistent theoretical framework for plasma-assisted ignition and combustion. Section 3 summarizes the different modeling strategies. Finally, section 4 develops a general theory for nanosecond plasma discharges, plasma-assisted ignition, and plasma-assisted premixed and non-premixed flames.

2. Theoretical framework

This section covers the physical configurations under consideration, the governing equations and their boundary conditions, the necessity for at least 1D modeling, and plasma-combustion chemistry.

2.1. Physical configurations

Three configurations are considered to study the effects of non-equilibrium plasma discharges on ignition, premixed flames, and non-premixed flames.

The first configuration [23, 27, 29, 30], shown in figure 1(a), is designed to simulate plasma discharges of fuel/oxidizer/diluent mixtures for low-temperature fuel oxidation and ignition. It is a plane-to-plane geometry to mimic nanosecond dielectric barrier discharge (NS DBD) reactor experiments [16, 17, 30, 35]. Two copper electrodes coated by thin dielectric layers are placed 1–1.5 cm apart, with the gap between them filled with gas mixtures. A high voltage power supply is connected to the right electrode, while the left electrode is grounded.
The second configuration [28], shown in figure 1(b), treats a plasma-assisted laminar flat premixed flame, simulating the McKenna burner experiment [36]. The entire flame is encapsulated in the plasma discharge. The burner exit serves as the ground electrode, and the high-voltage electrode, which is a perforated metal plate, is located 4 cm above the burner exit.

The third configuration [26, 37], shown in figure 1(c), simulates plasma-assisted non-premixed flames in counterflow experiments [38]. Two wire-mesh electrodes covered with thin alumina as dielectric layer (1.5 mm in thickness) are placed 1 cm apart in a tube filled with oxidizer. In this configuration, the discharge region is separated from the oxidizer burner exit. Thus, the residence time is large enough for gas temperature and species concentration to become uniform at the cross section of the oxidizer burner exit, to support the 1D assumption in this study.

2.2. Governing equations

A two-temperature non-equilibrium plasma model is developed, in which ions and neutral species are in thermal equilibrium at the gas temperature \( T \) [39], and electrons are in thermal non-equilibrium with the electron temperature \( T_e \) approximated by the ‘local electron mean energy method’ [40]. The governing equations include the Poisson equation for electric potential, the electron energy equation, and transport equations for charged and neutral species, as equations (1)–(3), respectively:

\[
\nabla \cdot (e \nabla \phi) = -e (n_+ - n_- - n_e) \tag{1}
\]

\[
\frac{\partial n_e}{\partial t} + \nabla \cdot J_e = \dot{Q}_e \tag{2}
\]

\[
\frac{\partial n_k}{\partial t} + \nabla \cdot J_k = \dot{\omega}_k. \tag{3}
\]

Electric field \( E = -\nabla \phi \) and energy input is thus calculated, rather than pre-specified as in the 0D models [17]. The transport of energy and species is treated using the drift (mobility)-diffusion model. The electron energy density is \( n_e \epsilon_e \).

The source term \( \dot{Q}_e \) is defined as

\[
\dot{Q}_e = \left( \frac{3k_B m_e}{e^2 M} \right) n_e \nu_{el} (T_e - T) - \sum \Delta E_{iri} - \sum J_e \cdot E. \tag{5}
\]

Here, the first term on the right-hand side represents the electron energy loss from elastic collisions with gas molecules. The second term characterizes the energy loss from electron impact reactions. The third term denotes the energy gain from the acceleration in the applied electric field. For species transport equations, the flux term \( J_k \) is defined as

\[
J_k = q_k \mu_k n_k E - \nabla (D_k n_k) + n_k u. \tag{6}
\]

The electron transport and reaction-rate coefficients are fitted as functions of electron energy \( \epsilon_e \) calculated by solving the electron Boltzmann equation with two-term expansion using the BOLSIG software [41], and renewed by interpolation at every time step and every spatial grid-point.

The gas flow is governed by the conservation equations of mass, momentum and total energy, as equations (7)–(9), respectively:

\[
\nabla \cdot (\rho \mathbf{u}) = 0 \tag{7}
\]

\[
\nabla \cdot (\rho \mathbf{u} \mathbf{u}) = -\nabla p + \nabla \cdot (\tau) + \rho \mathbf{F} \tag{8}
\]

\[
\nabla \cdot (\rho c_T \mathbf{u} T) = \nabla \cdot (\mathbf{F}_T) + \dot{Q}_e + \sum J_k \cdot E \tag{9}
\]
\[
\frac{\partial \rho}{\partial t} + \frac{\partial (\rho u_i)}{\partial x_i} = 0
\]  
(7)

\[
\frac{\partial \rho u_i}{\partial t} + \frac{\partial (\rho u_i u_j)}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{\partial q_i}{\partial x_i} + F_{ij}^{\text{EHD}}
\]  
(8)

\[
\frac{\partial \rho E}{\partial t} + \frac{\partial (\rho E + \rho p u_i)}{\partial x_i} = -\frac{\partial q_i}{\partial x_i} + \frac{\partial (u_i \tau_{ij})}{\partial x_j} + \dot{Q}^{\text{EH}}.
\]  
(9)

Following classical thermodynamics, the total energy \(\rho E\) is defined as

\[
\rho E = \rho h - p + \frac{\rho (u_i u_j)}{2}
\]  
(10)

where the mixture enthalpy is defined as

\[
h = \sum_k Y_k \left\{ h_k^0 (T_{\text{ref}}) + \int_{T_{\text{ref}}}^{T} C_{\rho,k} (T')dT' \right\}
\]  
(11)

The stress tensor \(\tau_{ij}\) is defined as

\[
\tau_{ij} = \kappa \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)
\]  
(12)

and the energy flux \(q_i\) from heat conduction and species diffusion is defined as

\[
q_i = -\lambda \left( \frac{\partial T}{\partial x_i} \right) + \rho \sum_k h_k Y_k \frac{\partial Y_k}{\partial x_i}.
\]  
(13)

Two special terms are introduced for plasma. The electrohydrodynamic force term \(F_{ij}^{\text{EHD}}\) is defined as

\[
F_{ij}^{\text{EHD}} = \varepsilon E_i (n_+ - n_- - n_e)
\]  
(14)

The Joule heating rate \(\dot{Q}^{\text{EH}}\) is defined as

\[
\dot{Q}^{\text{EH}} = eE \sum (J_+ - J_- - J_e).
\]  
(15)

Unlike equilibrium plasma, which transfers electrical energy only into sensible enthalpy, non-equilibrium plasma transfers electrical energy into the total energy of the gas mixture, and this triggers both gas temperature rise and chemical reactions. Heat release from chemical reactions is implicitly included in the unsteady term of the total energy equation, in the form of chemical energy being converted into sensible enthalpy.

### 2.3. Boundary conditions

Electric potential \(\phi\) is set to zero at the left boundary, and to the gap voltage \(V_{\text{gap}}\) at the right boundary. Gap voltage \(V_{\text{gap}}\) is calculated from the applied voltage \(V_{\text{app}}\) by solving the following equation [42]:

\[
\frac{dV_{\text{app}}}{dt} = \left( 1 + \frac{2la}{\varepsilon_d L} \right) \frac{dV_{\text{gap}}}{dt} - \frac{2la e}{\varepsilon_d a L} \int_0^L [J_+ - J_-] dx.
\]  
(16)

In the simulations, as shown in figure 2, a Gaussian fit of the experimental pulse waveform is used as the applied voltage \(V_{\text{app}}\). It is worth noting that the input pulse energy and ignition characteristics have been found to be highly sensitive to uncertainties in dielectric properties [27].

![Figure 2. Example of Gaussian fit of experimental pulse waveform used in simulation [29].](image)

Zero wall flux is enforced for all neutral species. The wall fluxes for electrons, positive ions, negative ions, and electron energy are specified by equations (17)–(20), respectively [43]:

\[
J_{e,s} \cdot n_s = \frac{1}{4} n_e \sqrt{\frac{8 k_b T_e}{\pi m_e}} + (a - 1) \mu_e n_e E \cdot n_s
\]  
(17)

\[
J_{+,s} \cdot n_s = \frac{1}{4} n_+ \sqrt{\frac{8 k_b T_+}{\pi m_+}} + a n_+ E \cdot n_s
\]  
(18)

\[
J_{-,s} \cdot n_s = \frac{1}{4} n_- \sqrt{\frac{8 k_b T_-}{\pi m_-}} + (a - 1) n_- E \cdot n_s
\]  
(19)

\[
J_{e,s} \cdot n_s = \left( \frac{1}{2} k_b T_e \right) \left[ \frac{1}{2} n_e \sqrt{\frac{8 k_b T_e}{\pi m_e}} + (a - 1) \mu_e n_e E \cdot n_s \right] - a \left( \frac{1}{2} k_b T_+ \right) \sum_k \gamma J_{+k,s} \cdot n_k
\]  
(20)

where the secondary electron emission coefficient \(\gamma\) is assumed to be 0.05 [43]. The temperature of the secondary electrons ejected from the electrode surface \(T_e\) is set to 1 eV [43]. In addition, \(a = 1\) if \(E \cdot n_s < 0\), and \(a = 0\) otherwise.

Zero wall flux is enforced for mass and momentum equations. The gas temperature boundary condition is set to be the analytic self-similar solution of the transient temperature distribution in a semi-infinite solid with constant heat flux [44]:

\[
T_b = \frac{T_{\text{amb}} + G(t) \times T_{\text{ew}}}{1 + G(t)} \quad G(t) = \frac{4k_g \sqrt{\alpha_d / \pi}}{k_d \Delta x}.
\]  
(21)

In practice, this boundary is closer to isothermal than to adiabatic conditions.

### 2.4. Necessity for one- and multi-dimensional modeling

The governing equations and boundary conditions described in the previous sections indicate that modeling must be at least 1D to capture cathode sheath formation and to calculate \(E/N\) accurately, where 0D models pre-specify it. As shown in figure 3, the sheath is the boundary between the plasma and the electrodes, with large electric field and electron number density gradients. In fact, rapid gas heating through ion Joule
effect mostly occurs inside the sheath boundary rather than in the bulk plasma [23]. Such heat adition is rapidly dissipated to the wall, because the boundary is approximately isothermal instead of adiabatic. Conductive heat loss to the walls, together with thermal diffusion into the bulk gas, prevents the overheating of the cathode sheath layer and the formation of ionization instabilities [23]. For this reason, the input energy matching in 0D models often results in over-prediction of the gas temperature of the bulk plasma.

To demonstrate the necessity of 1D modeling, Yang et al [29] directly compared the results from 1D and 0D models of nanosecond pulsed plasma-activated C2H4/O2/Ar mixtures, using the same plasma-combustion chemistry. For all quantities, the 1D model provides significantly better predictions than the 0D model, with respect to experimental measurements. Further analysis indicated that the kinetics pathways of fuel dissociation and oxidation are similar, but different pathways dominate in the two models.

2.5. Plasma-combustion chemistry

In this study, air or O2/Ar serve as the oxidizer and diluent (background gas), and a wide range of fuels is investigated, including hydrogen (H2), ethylene (C2H4), dimethyl ether (DME: CH3OCH3), and n-heptane (n-C7H16). DME and n-heptane are hydrocarbon fuels with low-temperature (below 700–800 K) chemistry (LTC) behavior. Reaction rate constants of electron impact reactions are calculated at each spatial grid-point and time step using BOLSIG [41] and modeled as functions of electron energy ϵe.

The chemical kinetics models for air-plasma [23] and O2/Ar plasma [29] are reduced from a detailed mechanism [15] via sensitivity analysis. The model includes neutral species N, N2, Ar, O, O2, O3, and NO; the charged species e−, N2+, N3+, Ar+, O2+, O3+; and O2; and electronically excited species Na(A*Σ), N2(B*Π1), N2(C*Π2), N2(A′ΣΣ), Ar*, O2(a′Δ), O2(b′Δ), O2(c′Σ), N(2D), and O (1D). CARS measurements of nitrogen vibrational temperature in air [20] indicated that the vibrational non-equilibrium is insignificant and not likely to affect the plasma chemistry, due to the fast vibrational relaxation within O (10 ns) [45, 46]. Therefore, vibrational excited species are not explicitly included in the model. For electron impact reactions, self-consistent sets of electron impact cross-sections are used for O2 [47], N2 [48], and Ar [49]. The rate constants of reactions between Ar+ and O2 were taken from Sun et al [50].

For H2 fuel, a chemistry model [27] is reduced from the above-mentioned plasma air chemistry, classical H2/O2 ignition kinetics [51], and H2 plasma reactions [52, 53] through sensitivity analysis. In addition to those species in the air-plasma chemistry, this reduced mechanism also includes neutral species H2, H, OH, HO2, and H2O, and charged species HN+3, and H3O+. For C2H4 fuel, the performance of two models, HP-Mech [17] and USC Mech-II [54], was compared for the prediction of nanosecond pulsed plasma activated C2H4/O2/Ar mixtures [29]. The predictions from HP-Mech were found to be better than those of USC Mech-II in terms of comparison with the experimental measurements, mainly because USC Mech-II does not include the high-pressure/low-temperature reaction pathway OH + C2H4 → CH2CH2OH. The C2H4 excitation cross-sections were estimated based on Janev and Reiter’s method [55].

For DME and n-C7H16 fuels, two chemical models [30, 56, 57] were developed based on a DME combustion model [58] and a reduced n-C7H16 model [59, 60]. In addition to H2/air plasma-combustion chemistry, these mechanisms also include the charged species CH+3, CH3OCH+2, CH3OCHH+3, C2H+5, C2H4+3, C2H5+1, and many neutral species. There are, however, no available cross-section data of electron impact reactions for DME and n-C7H16. It is assumed that their cross-sections are similar to that of C2H6 [61], which has a similar molecular structure. A sensitivity analysis was conducted by varying (up to 5 times) the rate constants of electron impact and quenching reactions, and a negligible impact on ignition delay predictions was observed [56].

Past studies [62] proved that the dominant reaction pathway for atomic oxygen (O) generation is e + O2 = e + O + O (1D), which means that almost half of the O produced by plasma is O (1D). In typical plasma-assisted ignition and combustion conditions, the high concentration of hydrocarbons result in much faster reactions between O (1D) and hydrocarbons (approximately 4 times) than the quenching of O (1D) to O [29], and should be added to the plasma-combustion chemistry models.

3. Numerical modeling strategies

The conservation equations of mass, momentum, energy, and neutral species are spatially discretized using a central scheme with the total variation diminishing (TVD) property [63]. The charged species equations derived from the drift (mobility)-diffusion model are spatially discretized using an exponential Scharfetter–Gummel scheme [64]. The numerical mesh is clustered toward the two electrodes to resolve steep gradients inside the sheath layers.

3.1. ‘Frozen electric field’ strategy

The ‘frozen electric field’ strategy takes advantage of the quasi-periodic behaviors of the electrical field to avoid recalculating the electric field for each pulse.
The transport equation of electron number density and the Poisson equation for electric potential are strongly coupled, which results in a severe time-step restriction. To handle this issue without affecting the accuracy, a semi-implicit form of the Poisson equation \([65]\) is solved using the implicit lower upper (LU) factorization method. The transport equations of electron number density and electron energy density are time-advanced using an implicit generalized minimal residual (GMRES)-based ODE solver \([66]\).

Under repeated nanosecond discharge, the electrical characteristics (input energy, \(E/N, n_e, n_c\), etc) of the non-equilibrium plasma present quasi-periodic behaviors, as shown in figure 4. Taking advantage of this behavior, the electrical characteristics do not need to be re-calculated every pulse, which significantly reduces computation time. More importantly, the stiffness of the system can be reduced dramatically, and the stringent time step size of \(0 (0.1–1) \text{ ps}\) during each pulse can be relaxed to \(0 (0.1–1) \text{ ns}\). Detailed evaluations \([24, 29]\) show that the electrical characteristics are not exactly periodic but approach quasi-periodicity after a certain number of pulses. After the plasma has reached this quasi-equilibrium, the input energy per pulse saturates to a constant value, thus the accumulated input energy is linearly proportional to the number of pulses. Based on this observation, a ‘frozen electric field’ strategy \([24]\) is implemented.

This strategy contains three steps. First, several discharge pulses are simulated based on the full model, until \(\Delta n_{e,\text{max}} \leq 5\%\). Second, the temporal-spatial distributions of \(E/N, n_e, n_c\) during the first pulse reaching \(\Delta n_{e,\text{max}} \leq 5\%\) are saved in a look-up table. Last, in all the following pulses, the Poisson equation for \(\phi\) and the transport equations of \(n_e\) and \(n_c\) are turned off, with the values of \(E/N, n_e, n_c\) frozen at the values in the table. In most cases, approximately 10 pulses are adequate to reach the quasi-equilibrium. Therefore, the speed-up factor from this strategy is approximately a tenth of the total number of pulses. The accuracy of this strategy has been verified and validated for a wide range of conditions \([24]\).

3.2. Correlated dynamic adaptive chemistry and transport (CO-DAC) strategy

A fractional time-step Strang-splitting scheme \([67]\) is employed to separate the convection–diffusion terms and the chemical source terms in the transport equations of neutral and ion species. The convection–diffusion terms are time-advanced using an explicit 4th-order Runge–Kutta method. The chemical source terms are time-advanced implicitly using the classical variable coefficient stiff ODE solver (VODE) \([68]\). The subroutines for the plasma chemistry mechanism are generated from an open-source 0D plasma kinetics solver, ZDPlasKin \([69]\). Numerical diagnostics indicate that more than half of the computation time is spent on the implicit time-integration of chemical source terms. To tackle this issue, several acceleration techniques are proposed and employed with extensive verification \([25]\).

Firstly, the point-implicit stiff ODE solver (ODEPIM) \([25, 70–73]\), a semi-implicit solver, is employed to replace the purely implicit VODE solver. Providing similar accuracy, ODEPIM is approximately 60 times faster than VODE.

Since the computation time for chemistry is (linearly to cubically) proportional to the number of species, a dynamic adaptive chemistry (DAC) \([74]\) technique is proposed. DAC generates a locally reduced kinetics mechanism for each spatial location and time step. Only the reaction rates of selected species and reactions are calculated, and the rest are frozen. To reduce the large computational overhead for local mechanism reduction, a correlated version of DAC (CO-DAC) \([25, 71–73, 75]\) is proposed to create time-space correlation zones with similar thermo-chemical states, with only one time local reduction needed for each zone. CO-DAC is eminently suitable for the problems shown in figure 1, because of the uniformity of the bulk plasma and the quasi-periodic behaviors of the discharge. CO-DAC further speeds up the chemistry calculation by a factor of approximately 3 with negligible computational overhead.

Equipped with ODEPIM and CO-DAC, the dynamic evaluation of mixture-averaged transport coefficients (viscosity, thermal conductivity, and species diffusivity) becomes a large portion of the total computation time. Using the same correlation technique as in DAC but different zone grouping criteria \([25, 71, 72, 76]\), the calculation of mixture-averaged transport coefficients is reduced by more than 800 times with negligible computational overhead.

3.3. Three-stage multi-time scale modeling strategy

Plasma-assisted ignition and combustion take place over a broad range of time scales. The ionization wave propagation, electrical breakdown, cathode sheath formation, and electron impact reactions have characteristic time scales at the sub-nanosecond level. Fast gas heating from the quenching of excited species and ion recombination has characteristic time scales on the order of microseconds. The cumulative effects of repetitive pulses, convective and diffusive transport, and ignition and combustion, occur in the range from milliseconds to seconds.

In nanosecond pulsed plasma discharges, the sub-nanosecond scale physical processes occur within each pulse. The microsecond level processes occur primarily during gaps between adjacent pulses. The millisecond to second scale processes occur generally after the accumulation of a significant number of pulses. To utilize this decoupling of time scales, a two-level adaptive time-step approach \([23, 77]\) is proposed,
and it is extended to a three-level version for computationally efficient simulation of ignition [57].

During each voltage pulse, all equations are solved simultaneously, and the time step size is set to O (0.1–1 ps). The exact time step size is dynamically determined based on the strength of Ein, the electron number density, and the Courant–Friedrichs–Lewy (CFL) condition for convection–diffusion terms.

In the duration between two consecutive pulses, both applied and gap voltages are nearly zero. As a result, the charge density quickly vanishes, and the electric field and its influence become negligible. The Poisson equation for electric potential and the electron energy equation are turned off, and the electric field and total charge are set to zero. This significantly reduces the stiffness of the system, such that the time step size can be increased to O (0.1–1 ns) without sacrificing accuracy or triggering numerical instability. The time step size is reset to O (0.1–1 ps) at the start of the following pulse, and this procedure is repeated until all pulses are finished.

After all pulses are completed, the time step of O (0.1–1 ns) is still too small to reach ignition in times on the order of 1–1000 ms within a reasonable computation time. To handle this issue, the transport equations of all charged species (electrons and ions) are turned off to further reduce the stiffness, so that the time step could be further increased to O (10–100 ns) [57] without sacrificing accuracy or triggering numerical instability.

4. General theory

In this section, a general theory of plasma-assisted ignition and combustion is established, based on results from high-fidelity modeling and simulations. The framework consists of three components. The first component is a multi-time scale theory for nanosecond pulsed plasma discharges. The second component is a theory of plasma-assisted ignition, including one- and two- stage ignition, and the propagation of the ignition kernel. The last component is a theory of plasma-assisted flames, including both premixed and non-premixed flames.

4.1. Nanosecond pulsed plasma discharges: a multi-time scale theory

Previous studies [23, 29, 30, 37, 77, 78] on the nanosecond pulsed plasma discharge of air and fuel/oxidizer/diluent mixtures have provided very detailed information about the underlying physical processes. Here we establish a general theory of nanosecond discharges based on existing literature and our model results.

Because of the multiscale nature of plasma, it is convenient to differentiate the key physical processes based on their characteristic times. The characteristic time scale $\tau_k$ for the decay of the $k$th species can be estimated as

$$\tau_k = \left(\frac{\partial}{\partial Y_k} \left( \frac{dY_k}{dt} \right) \right)^{-1} = \left( \frac{\partial \text{Dec}_k}{\partial Y_k} \right)^{-1} \tag{22}$$

where the decay rate $\text{Dec}_k$ is defined as the rate sum of all reactions with the $k$th species as a reactant [79]. As an example, the temporal decay of electrons, H, O, and OH radicals is shown in figure 5 to indicate the different ranges of time scale involved. Since physical time scales depend on pressure (collision rates), the pressure range is specified as 60–150 Torr. The pulsed discharges in this study have discharge durations of O (10 ns) and frequencies of 10–100 kHz. The gap between two adjacent pulses is of O (10–100 $\mu$s), and O (100) pulses could finish within a few ms.

The multi-time scale theory for nanosecond pulsed plasma discharges is summarized in table 1. The underlying physical processes are categorized into four stages with drastically different time scales. The first stage is the discharge pulse, which has time scales of O (1–10 ns). The second stage is the afterglow phase in the gap between two adjacent pulses, which has time scales of O (100 ns). The third phase is the remaining gap between pulses, which has time scales of O (1–1000 $\mu$s). The fourth stage is the completion of O (100) pulses, which has time scales of O (1–1000 ms). Details of the physical processes in each stage will be discussed in the following sections.

4.1.1. Stage I—discharge pulse. During this stage, the discharge pulse deposits electrical energy into the gas mixture, which becomes the source of the non-equilibrium plasma. The energy deposition depends primarily on the ionization rate of the background gas. For most mixtures of fuel/oxidizer/diluent, the normal background gases are oxidizer and diluent, because of the low concentration of fuel (typically a few percentage by mole-fraction). Therefore, a change of fuel type has very limited influence on the energy deposition [37]. For a fixed peak voltage $V_{\text{peak}}$, the electrical energy deposition per pulse $Q_{\text{pulse}}$ is linearly proportional to the capacitor current, which is equal to the capacitance times the time rate of change in voltage ($V_{\text{peak}}/t_{\text{pulse}}$) across the capacitor. In particular, based on a parametric study for $V_{\text{peak}}$ from 10 kV to 90 kV, Nagaraja and Yang [37] proposed that for a pressure of 50 Torr and an initial gas temperature of 300 K,

$$Q_{\text{pulse}} = 0.14 \left( \frac{V_{\text{peak}}}{t_{\text{pulse}}} \right) + 0.64 \tag{23}$$

$Q_{\text{pulse}}$ is also proportional to pressure and thus particle number density, but only a weak function of pulsing frequency [23]. In
out of the sheath layers into the bulk plasma with high energies of 10–100 eV [26].

Under the high (30 kV) potential, the electric field inside the sheath layers continues almost immediately after breakdown (figure 2). As shown in figure 3, the electric field intensity increases rapidly due to the increase in the applied voltage, which results in rapid ion Joule heating inside the sheath layers to increase with further increase in applied voltage, which is not dependent on gas temperature, and this is partially why electron impact reactions are the most important processes in this stage. Electron impact reactions are fast electron impact reactions, which are the most important processes in this stage.

In contrast, the range of $E/N$ depends strongly on pulsing frequency [78]. More precisely, as shown in figure 6, higher frequency has lower peak value for the primary spike but higher peak values for the secondary spikes. This is because higher pulsing frequency increases the residual electron density and serves as a uniform pre-ionization source, which lowers the breakdown voltage.

Figure 7 shows that vibrational excitation dominates the input energy coupling when $E/N$ is smaller than 100 Td, while electronic excitation dominates when $E/N$ is greater than 100 Td [23]. For this reason, secondary spikes in the $E/N$ profile represent pure vibrational energy coupling, and higher frequency pushes more input energy into vibrational excitation, which quickly relaxes and contributes to the fast gas heating for bulk plasma [80].

During the high voltage pulse, the fast ionization wave during the primary breakdown (60–75% of input energy coupling) results in nearly uniform plasma discharge. The charge surge inside the sheath layers form a strong shield, which makes $T_{gas}$ and the electric field in the bulk plasma drop almost immediately after breakdown (figure 2). As shown in figure 3, the electric field intensity inside the sheath layers continues to increase with further increase in applied voltage, which results in rapid ion Joule heating inside the sheath layers (30–40 K within 80 ns) [23]. Under the high $E/N$ inside the sheath layers, the electrons are accelerated significantly to fly out of the sheath layers into the bulk plasma with high energies of 10–100 eV [26].

The large number of high-energy electrons triggers ultrafast electron impact reactions, which are the most important processes in this stage. Electron impact reactions are not dependent on gas temperature, and this is partially why plasma can trigger/sustain low-temperature ignition/combustion. These reactions can be classified into two categories: electron impact excitation and electron impact dissociation. The former one uses more than half of the input energy [26] and efficiently generates electronically excited $O_2$ and $N_2$/Ar species, including $O_2(a^1 \Delta), O_2(b^1 \Sigma), O_2(c^1 \Sigma), N_2(A^3 \Sigma), N_2(B^1 \Sigma), N_2(C^1 \Pi), N_2(d^1 \Sigma), Ar^*$. In most cases, the concentration of diluent ($N_2$/Ar) is higher than $O_2$, so the concentration of excited $N_2$/Ar is also higher than that of excited $O_2$. Electron impact dissociation reactions dissociate $O_2$ into $O, O (1D)$, and $O (1S)$, which contributes 40–70% of $O$ generation and part of

<table>
<thead>
<tr>
<th>Time scales (60–150 Torr)</th>
<th>Stage (10–100 kHz)</th>
<th>Key processes and mechanisms</th>
<th>Oxidizer and diluent</th>
<th>Fuel</th>
<th>Gas heating</th>
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<tr>
<td>O (1–10 ns)</td>
<td>Discharge pulse</td>
<td>Primary breakdown (60–75% of input energy coupling) Fast ionization → uniform discharge</td>
<td>Excitation (&gt;50% of input energy) Electron impact dissociation: $O_2 \rightarrow O + O (1D)$ $O (1D) + fuel$: $H$ abstraction $\rightarrow OH$ dissociation or pyrolysis</td>
<td>H abstraction $\rightarrow H$ (re-activate LTC) dissociation</td>
<td>Electron impact dissociation Vibration relaxation</td>
</tr>
<tr>
<td>O (100 ns)</td>
<td>Afterglow</td>
<td>Quenching of excited species (weak $T_{gas}$ dependence) Dissociation via quenching of excited species: $O_2 \rightarrow O + O (1D)$</td>
<td>$O + OH + H_2 \rightarrow O_2 + OH/H_2O$ O/OH + fuel: $H$ abstraction $\rightarrow OH/H_2O$ dissociation or pyrolysis $\bullet$ Partial oxidation</td>
<td>Fast gas heating (0.5–2 K per pulse)</td>
<td></td>
</tr>
<tr>
<td>O (1–100 μs)</td>
<td>Remaining gap between pulses</td>
<td>Chain propagation &amp; termination (sensitive to $T_{gas}$) Exothermic chain termination</td>
<td>$O_2 + fuel$ fragment $\rightarrow H \rightarrow HO_2$ $Ho/HHO_2 \rightarrow O_2 + OH/H_2O$</td>
<td>$O_2$ dissociation $\rightarrow OH/H_2O$ dissociation or pyrolysis $\bullet$ Partial oxidation ** Large pool of radicals &amp; fuel fragments (enhance/re-activate LTC) Exothermic $O_2/CO$ formation &amp; partial oxidation Uniform $T_{gas}$ profile, volumetric heating</td>
<td></td>
</tr>
<tr>
<td>O (1–1000 ms)</td>
<td>O (100) pulses or after all pulses</td>
<td>Slow/weak process (sensitive to $T_{gas}$) Convection &amp; diffusion</td>
<td>$O + O_2 + M \rightarrow O_3 + M$ dissociation or pyrolysis $\bullet$ Partial oxidation $\bullet$ $CO \rightarrow CO_2$ exothermic $O_2/CO$ formation &amp; partial oxidation $\bullet$ Uniform $T_{gas}$ profile, volumetric heating</td>
<td></td>
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Table 1. Multi-time scale theory for nanosecond pulsed plasma discharges.
the fast gas heating in bulk plasma [23, 29]. O + O (1D) is the dominant product combination of the electron impact dissociation of O2 [62]. Electron impact can also dissociate N2 into N and N (2D) [56], but the rates of these dissociation reactions are significantly lower than those of O2 because of the strong triple bond in N2. The electron impact on fuel molecules can trigger H-abstraction and dissociation/pyrolysis of fuel. The electron impact reaction dissociates H2 fuel into two H radicals, which partially replaces the original chain initiation reactions in classical H2 combustion kinetics with high activation energies [37]. The electron impact reactions abstract H from C2H4 fuel molecules to produce fuel fragments C2H3 and C2H2, and this contributes more than half of the H radical generation [29]. For fuels with LTC, electron impact reactions abstract H from fuel molecule RH (for example, fuel radical R is C8H15 for n-heptane, and is CH3OCH2 for DME) to produce R and H radicals, which can re-activate LTC for initial gas temperatures higher than the typical LTC threshold temperature (such as 800 K at a reduced pressure of 76 Torr) [34, 57].

The fast reactions between O (1D) and fuel can result in further H-abstraction and dissociation/pyrolysis of fuel molecules, which are approximately 4 times faster than the quenching of O (1D) to O radical [29]. For H2 fuel, a low-temperature chain propagation reaction O (1D) + H2 → OH + H is introduced, which is more than two orders of magnitude faster than the classical chain propagation reaction O + H2 → OH + H and dominates the OH radical production for the first few pulses [37]. For C2H4 fuel, the H-abstraction reaction C2H4 + O (1D) → C2H3 + OH produces approximately 25% of OH radical generation; the dissociation reactions C2H4 + O (1D) → CH2 + CH2O and C2H4 + O (1D) → CH3 + HCO produce 63% of CH2, 17% of CH2O (a typical marker species for LTC), 60% of CH3, and 20% of HCO [29]. For fuels with typical LTC, O (1D) abstracts H from fuel molecule RH to produce R and OH radicals, which contributes more than half of the O (1D) consumption [30, 34].

4.1.2. Stage II—afterglow. Quenching of N2(a1Σg, B′Π, C′Π, a′1Σg) or Ar* from Stage I further dissociates O2 into O, O (1D), and O (1S), which contributes approximately 60% or 30% of O production, respectively [23, 29]. This indicates that either the production rate of excited N2 is larger than that of excited Ar, or the excited N2 is more active than excited Ar. In addition, O + O (1D) is the dominant product during the dissociation of O2 from quenching of excited dilute species. This quenching is approximately 4 times slower than the reactions between O2 and fuel molecules in Stage I [29]. The quenching also introduces several new NOx formation pathways: N2(Δa1Σg) + O → NO + N (2D) and N (2D) + O2 → NO + O [56]. Although linearly proportional to the number of discharge pulses [53, 56], the amount of NOx introduced by these new pathways is significantly smaller than the decrease in NOx from the plasma-assisted ultra-lean combustion [5]. The quenching can also result in fuel dissociation/pyrolysis. In particular, the quenching of N2(a1Σg) can dissociate H2 into 2H, which partially replaces the original chain initiation reactions in classical H2 combustion kinetics with high activation energies [37]. Quenching of the excited species is the major source for fast gas heating of 0.5–2 K per pulse inside the bulk plasma [27, 78, 80], and consumes 20–40% of the discharge energy [29, 80].

In this stage, in addition to quenching, there is conversion of one excited species into another excited species. The major conversion pathways are O (1S) → O (1D) and O2 (c1Σg) → O2 (b1Σg) → O2 (a1Δg) [29].

As shown in figure 5, the electron-ion recombination reactions have a time scale of O (100 ns) [26, 29], which is defined as the time for electron number density to reach its initial levels, thus occur primarily in this stage. Electron-ion recombination reactions contribute part of the fast gas heating of the bulk plasma, and some of them may trigger further decomposition: e + O3+/N2+ → 2O/2N [26]. Reactions in this stage have only weak gas temperature dependence, which is partially why plasma can trigger and sustain low-temperature ignition and combustion.

4.1.3. Stage III—remaining gap between pulses. In the third stage, O2 reacts with fuel fragments (such as HCO) or H radical to generate HO2, one of the most important species for LTC. For hydrogen fuel, the three-body reaction H + O2 + M → HO2 + M is the primary source of HO2 [27]. For hydrocarbon fuels, this reaction is still primary under high pressures, but HCO + O2 → CO + HO2 becomes the primary source of HO2 and CO under low pressures (that is, ~90% of HO2 and >80% of CO under 60 Torr) [29]. HO2 is quasi-stable and reacts significantly slower than the other radicals at low gas temperatures, so its reactions occur primarily in this stage. Highly exothermic radical reactions with HO2 (O/H + HO2 + O2 + OH/H2O) are significantly faster than those with fuel molecules, and dominate the OH radical production after approximately 0.1 ms (that is, after a few pulses) and contributes part of the gas heating in the bulk plasma [27, 37]. In addition, the reaction rates of radicals with HO2 are proportional to pressure, but insensitive to equivalence ratio [24]. HO2 also plays a role in NOx conversion and generates more OH radical: NO + HO2 → NO2 + OH [56].

In this stage, gas temperature sensitive reactions between radical and fuel further contribute the H-abstraction, dissociation/pyrolysis, partial oxidation, and thus part of the gas heating in the bulk plasma. For C2H4 fuel, reactions between O and C2H4 include both H-abstraction (O + C2H4 → H + CH3CHO) and dissociation (O + C2H4 → CH3 + HCO), both of which are
also partial oxidation and release heat to the bulk plasma. Under high-pressure or low-temperature reaction with CH₄ fuel consumes most of the OH radical, and the product CH₂CH₂OH is quasi-stable [29]. For fuels with typical LTC, radicals (O/H/ OH) abstract H from fuel molecule RH to produce R and OH/ H₂/H₂O, and release heat to the bulk plasma, contributing approximately 50% of the consumption of O radical, and most production and consumption of OH radical [30, 34].

Over the time scales of O (1 ms), the increase in gas temperature inside the sheath layers from the ion Joule heating in Stage I is rapidly dissipated, mainly to the cold electrode wall through heat conduction [23, 80]. This dissipation prevents the overheating of the sheath layers and the development of ionization instabilities.

4.14. Stage IV—completion of O (100) pulses. Under low pressures, the conversion between O and O₃ via O + O₂ + M ↔ O₃ + M is a relatively slow process, and can equal or exceed the production rate of O only at time scales of O (ms) [23]. In addition, the decay of O₂ (a¹Δ) and O₂ (b¹Σ⁺) is even slower than the formation and decomposition of O₃, on the order of O (1 s) and O (10 ms), respectively [29]. For combustion systems, in which plasma and flame are spatially decoupled (that is, not in situ), the relatively long lifetimes of O, O₂, and O₂ (a¹Δ) under low pressures makes them important carriers of the enhancement from plasma [26]. First, the plasma zone generates large amounts of O, O₂, and O₂ (a¹Δ). Then, the flow transports these species to the preheat zone of the flame. Finally, the high gas temperatures in the preheat zone decompose O₂ to generate more O radical, which significantly shortens the auto-ignition delays in the preheat zone and stabilizes the flame under ultra-lean conditions.

For CH₃CHO produced from Stage III can further react with O₂ to dissociate into CO, CH₂O, and OH, which contributes approximately 40% of OH radical generation [29]. Under low gas temperatures and short time scales, more than half of CO₂ production comes from CH₂ + O₂ → CO₂ + (H + H, H₂) [17, 29], rather than from the highly exothermic chain propagation reaction CO + OH → CO₂ + H, which is too weak and slow under such conditions [37].

Convection and diffusion processes also occur in this stage.

At the end of approximately 100 pulses with time scales of O (1 ms), a large pool of radicals and fuel fragments has been formed in the bulk plasma, accumulated from all the processes of Stages I-III [23], and a uniform ‘hat-shaped’ gas temperature profile has been developed. Since most of processes have weak gas temperature dependence or are even independent of gas temperature, plasma can trigger and sustain low-temperature ignition and combustion under ultra-lean combustion conditions.

4.2. Plasma-assisted ignition

Previous studies on plasma-assisted ignition [24, 27, 34, 56, 57, 80] provide detailed information about the underlying physical processes. For fuels with LTC, when the initial gas temperature is low enough, ignition takes place in two stages: first stage ignition to ‘cool flame’, and second stage ignition to hot flame [34]. For fuels without LTC, there is no first stage ignition or ‘cool flame’, and ignition is equivalent to the second stage. After second stage ignition, the ignition kernel propagates to form a relatively stable flame front. Thus, the physical processes can be divided into three stages: first stage ignition, second stage ignition, and the propagation of ignition kernel. The general theory for plasma-assisted ignition is summarized in table 2. The details of the physical processes of each stage will be discussed in the following sections. The pressure range of the present study is specified as 60–150 Torr, and the pulsed discharges have durations of O (10 ns) and frequencies of 10–100 kHz.

4.2.1. First-stage ignition to ‘cool flame’. Two-stage ignition and ‘cool flame’ are only present in fuels with LTC, such as DME and n-heptane. First stage ignition to ‘cool flame’ occurs through a self-sustaining exothermic LTC chain branching cycle (figure 8) [34]. The fuel molecule can be expressed as RH, where R is its corresponding fuel radical (R is CH₃OH₂ for DME, and C₇H₃ for n-heptane). First, H abstract reactions via radicals (such as O, H, OH) generate fuel radical R. Then, R reacts with O₂ to form RO₂, which then isomerizes to hydroperoxyl alkyl radical QOOH, where Q is the corresponding alkyl radical (Q is CH₂OH₂ for DME, and C₇H₁₂ for n-heptane). After that, QOOH adds another O₂ to form Q₂OQQO. Finally, Q₂OQQO isomerizes and decomposes to two OH radicals, which complete the chain branching cycle.

For initial gas temperatures below ~700–800 K, as shown in figure 9, the first stage ignition to ‘cool flame’ can occur without plasma. Therefore, the plasma enhancement has a catalytic effect and depends only weakly on the number of pulses [56]. Plasma initiates a small amount of seed radicals, such as O, H and OH, at the beginning, and this accelerates the H abstraction reactions from fuel molecules and triggers the self-accelerating LTC feedback loop. This significantly reduces (approximately 10 times) the induction time of the cycle. In this case (for a small number of pulses), the plasma enhancement of LTC is nearly independent of equivalence ratio. It is more pronounced at lower gas temperatures (550–650 K) because of the difficulty of initial radical production at low gas temperature conditions, where the LTC is stronger [56].

For initial gas temperatures above ~700–800 K, as shown in figure 9, there is no first stage ignition or ‘cool flame’ without plasma. This is because direct decomposition of fuel radical R into small alkenes (the yellow and red pathways in figure 8) is significantly accelerated at higher initial gas temperatures, and the LTC chain branching cycle, which has weak gas temperature dependence, is negligible. However, plasma discharges introduce ultra-fast H-abstraction reactions e/O (ΔDo + RH → R + (H + e)/OH to produce a large amount of R orders of magnitude faster than regular H-abstractions via radicals [57]. Due to the limited decomposition rate of R, a significant amount of R goes to the LTC cycle again, and the first stage ignition to ‘cool flame’ reappears, as shown in figure 9. The strength of this re-activated LTC cycle is linearly proportional to the accumulative input energy, as is the ‘cool flame’ temperature [57].
For all gas temperature ranges, when the number of pulses is large (approximately 50 pulses or more), plasma enhancement is more than just a catalytic effect, and the relationship between ‘cool flame’ temperature and accumulative input energy is linear even when the initial gas temperature is below ~700–800 K. In this case, the normalized first stage ignition rate $\tau_{self}/\tau_{plasma}$ (the reduction factor of the first stage ignition delay) is an exponential function of accumulative input energy [57]. The reason for this is that the reactivity to generate radicals and excited species is an exponential function of electron temperature at low gas temperatures, which is linearly proportional to input electrical energy. In this case, the reduction of the first stage ignition delay is significantly larger than in the pure catalytic case; for example, 150 pulses reduce ignition delay by approximately 250 times for a DME/O2/Ar mixture at 76 Torr [57].

4.2.2. Second-stage ignition to hot flame. The concept of the second-stage ignition is relevant to the two-stage ignition of fuels with LTC; the ignition of fuels without LTC can be considered as the second stage ignition. This stage can be further divided into two steps. In the first step, the gas-heating sources increase the gas temperature to beyond a threshold value (auto-ignition temperature). Below this threshold gas temperature, ignition will not occur because of the competition between quenching and radical production. In the second step, above the threshold gas temperature, chain branching and fuel oxidation pathways are triggered and accelerated until the process becomes self-sustaining, and the gas temperature continues to rise until the final ignition. For this reason,

<table>
<thead>
<tr>
<th>Stage</th>
<th>Fuel type</th>
<th>Stage initial T</th>
<th>Stage flame T</th>
<th>$\tau_{self}/\tau_{plasma}$</th>
<th>Key processes and mechanisms</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st stage ignition to ‘cool flame’</td>
<td>Fuels with LTC (e.g. DME, n-heptane)</td>
<td>&gt;~700–800 K; &lt;~700–800 K</td>
<td>Linear function of input energy &amp; initial T</td>
<td>$+\infty$</td>
<td>Exponential function of input energy</td>
</tr>
<tr>
<td></td>
<td>Fuels with LTC</td>
<td>~Adiabatic flame T</td>
<td>Exponential to ‘cool flame’ T &amp; input energy after 1st stage</td>
<td>Fast gas heating (0.5–2 K per pulse)</td>
<td></td>
</tr>
</tbody>
</table>
| Fuels without LTC | >Self-auto-ignition T | <Plasma auto-ignition T | Exponential function of input energy | Plasma/LTC $\rightarrow$ radicals $\rightarrow$ exothermic T-sensitive chain branching positive feedback cycle:  
- HO$_2$ $\rightarrow$ H$_2$O$_2$ $\rightarrow$ 2OH  
- Fuel dissociation or pyrolysis  
- Fuel oxidation |
| Between plasma & self-auto-ignition T | <Plasma auto-ignition T | No ignition |  |

**Table 2.** General theory for plasma-assisted ignition.

*Figure 8.* Schematic of the key reaction pathways for plasma-assisted fuel oxidation at different gas temperatures (blue arrow below 700K; yellow arrow 700–1050K; red arrow above 1050K). Note that critical gas temperature conditions are pressure dependent. e: energetic electrons, *: electronically excited molecules; v: vibrationally excited molecules [34]. [34] 2016 © Springer Science+Business Media New York 2015. With permission of Springer.

*Figure 9.* Comparison of gas temperatures for plasma-assisted stimulation (30kHz repetition rate) and auto-ignition of DME/O2/Ar mixture at 76 Torr pressure [57].
during this second step, the effect of plasma is negligible [27]. A threshold value exists because typical chain branching reactions are endothermic and highly gas temperature sensitive. A small increase in gas temperature near ignition significantly increases the chain branching reaction rates to produce radicals, which then accelerates the heat release from fuel oxidation. Consequently, the radical profiles are much steeper than their gas temperature counterpart. The increase in gas temperature completes the cycle by further increasing the rates of chain branching reactions. This non-linear positive feedback cycle causes an exponential increase in both gas temperature and radical concentrations, subsequently leading to ignition.

The presence of plasma can reduce the threshold auto-ignition temperature and enhance or shorten the first step but not the second step. For example, at pressures of 80–100 Torr, plasma reduces the auto-ignition temperature of lean H2/air mixtures (equivalence ratios of 0.06–0.12) from ~900 K to ~700 K, as shown in figure 10 [27]. As described in previous sections, fast gas heating of 0.5–2 K per pulse takes place in the bulk plasma, primarily from the quenching of excited species. In addition, the large pool of radicals and excited species generated by the plasma or the LTC chain branching cycle pre-activates the high-temperature chain branching and oxidation pathways (such as 2H2O → H2O2 + O2 and H2O2 → 2OH), which also release a large amount of heat. For a given type of nanosecond pulsed discharge, there exists a threshold number of pulses, or equivalently a threshold accumulative input energy, to trigger ignition. Plasma is thus seen to have a larger enhancing effect in the first stage [56, 57], where it can have catalyst effects, while the second stage depends on threshold-like behavior. For two-stage ignition of fuels with LTC, if the number of pulses after the first stage is small (20–30 pulses), then the radical pool directly introduced by plasma will be much smaller than that introduced by the LTC cycle of the ‘cool flame’. In that case, a plasma burst after the first stage ignition provides predominantly thermal enhancement, which only reduces the second stage ignition delay by approximately 30% [56].

As shown in figure 10, the ignition delay increases steeply as the number of pulses is reduced. The normalized ignition rate τ_self/τ_plasma (reduction in ignition delay) is an exponential function of accumulative input energy [27], because reactivity is an exponential function of electron temperature at low gas temperatures, and an exponential function of gas temperature at high gas temperatures, both of which are linearly proportional to input electrical energy. For fuels with LTC, this relation is equivalent to an exponential function of both ‘cool flame’ temperature and the accumulative input energy after the first stage[57], because the former one is linearly proportional to the latter one. When the number of pulses is small (within ~10 pulses), the discharge pulses applied at the beginning have negligible impact on the ‘cool flame’ temperature, and thus negligible impact on the second stage ignition delay [56]. In contrast, when the number of pulses is large (approximately 50 pulses or more), the LTC chain branching cycle is either significantly enhanced or re-activated, which generates a significantly larger radical pool and heat release than the un-enhanced or un-activated cycle and significantly reduces the second stage ignition delay. Taking a DME/O2/Ar mixture under 76 Torr and 150 discharge pulses as an example [57], for initial gas temperatures below ~700–800 K, the LTC chain branching cycle is only enhanced, so the ignition time reduction factor is only ~15. For initial gas temperatures above ~700–800 K, the LTC chain branching cycle is re-activated, so the reduction factor could be as large as ~75.

4.2.3. Ignition kernel propagation. Auto-ignition first occurs at the center of the discharge gap, where the gas temperature first reaches the reduced threshold value [27]. Nevertheless, assisted by plasma discharges, the gas temperature profile is close to uniform distribution [23, 29], such that other locations also reach the reduced threshold gas temperature rapidly (indeed, almost simultaneously). Auto-ignition occurs independently at different locations because the local preheated mixture is doped with radicals from the plasma discharge burst [80], such that heat transport does not play a significant role [27]. This is different from hot-spot thermal igniters, which require diffusion of both radicals and heat [80]. As a result, the ignition kernel expands rapidly to the entire volume, except near the quasi-isothermal walls, where the rapid heat conduction losses from the high gas temperature gradients keep the gas temperature low [23, 29]. Therefore, the plasma-assisted ignition kernel propagation speed is significantly faster than laminar flame speed (approximately 15 times faster for lean H2/air mixture at 80 Torr), and plasma can ignite the entire volume of premixed mixture significantly faster than thermal ignition but with smaller minimum ignition energy (MIE) [80].

4.3. Plasma-assisted flames

Previous studies on plasma-assisted flames investigated the two basic flame types: premixed [28] and non-premixed (diffusion) flames [26]. All other (practical) flames are combinations of these two basic flame types, so the plasma enhancement on them can be inferred. These studies provide detailed information about the underlying physical processes; here we summarize the findings to develop general theories for both types.

4.3.1. Premixed flame. In this study, due to the limitations of the 1D model, we only consider the laminar flat premixed flame, which is enhanced by in situ plasma discharges, as...
shown in figure 1(b). The premixed flame contains several zones: the pre-heat, reaction, and post-flame zones. In the laminar premixed flame, the reaction zone is very thin, so the volumetric plasma enhancement is not significant there. Near the burner, due to fast heat conduction to the wall, the gas temperature is lower than ~500 K, and several quasi-stable species are formed and last. Based on these analyses, we organize the general theory for plasma-assisted premixed flame into three zones: near the burner zone, pre-heat, and post-flame zones, which is summarized in table 3.

Figure 11 shows the spatial distributions of $E/N$, electron number density, OH concentration, and gas temperature in the presence of a lean premixed H$_2$/O$_2$/N$_2$ flame. $E/N$ varies inversely with N (proportional to the gas temperature at a constant pressure condition) during each pulse. Because of intense gas expansion from heat release, high $E/N$ (~700–1500 Td) regions are found downstream of the flame (in the high-temperature flame and post-flame zones). Inside the cathode sheath (near the boundary of the post-flame zone), $E/N$ attains its highest value of approximately 1500 Td for a short duration. In this range, as shown in figure 7, a significant fraction of the input energy goes to ionization, and thus less electron energy can go to electronic mode to generate radicals via electron impact reactions. In contrast, lower $E/N$ values (100–700 Td) in the low gas temperature pre-heat zone and near the burner push more energy into the electronic mode, which promotes more electron impact excitation and dissociation to generate radicals and excited species in an efficient manner. In figure 11(b), as a direct comparison, plasma increases OH concentrations by ~100–500% in the pre-heat zone, but only by ~40% in the post-flame zone. The largest increase of ~500% occurs near the burner surface. Increased OH concentrations enhance the heat release from the primary chain propagating oxidation reactions (OH + H$_2$/CO $\rightarrow$ H$_2$O/CO$_2$ + H). The resulting increase in gas temperature accelerates the conventional fuel oxidation chain branching, creating a positive feedback loop for radical production. With plasma discharge, gas temperatures increase by approximately 20% in both the pre-heat and post-flame zones, as shown in figure 11(b). Such difference in gas temperature could be attributed to the heat release triggered by partial oxidation of fuel molecules by plasma-generated radicals. Effects of both chemistry and direct gas heating are responsible for a significant portion of the plasma enhancement. In fact, non-equilibrium plasma generates considerably larger amounts of radicals than the same rate of indiscriminate gas heating. The plasma chemistry enhancement of the flame is more pronounced at fuel-lean conditions.

In the pre-heat zone, plasma discharges significantly increase O and H radicals, with the peak values increasing by factors of six and four, respectively. In addition, as shown

### Table 3. General theory for plasma-assisted premixed flame.

<table>
<thead>
<tr>
<th>Zone</th>
<th>Near the burner</th>
<th>Pre-heat zone</th>
<th>Post-flame zone</th>
</tr>
</thead>
<tbody>
<tr>
<td>T range</td>
<td>$\leq$~500 K</td>
<td>$\sim$500–700 K</td>
<td>Flame T</td>
</tr>
<tr>
<td>$\rho$ &amp; N</td>
<td>High</td>
<td>$\sim$700 K</td>
<td>Flame T</td>
</tr>
<tr>
<td>$E/N$ range</td>
<td>$\sim$100–700 Td</td>
<td>Flame T</td>
<td>~700–1500 Td</td>
</tr>
<tr>
<td>Dominant mode</td>
<td>Electronic</td>
<td>Ionization</td>
<td>~90%</td>
</tr>
<tr>
<td>Input energy</td>
<td>$\sim$10%</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Non-equilibrium</td>
<td>O$_3$</td>
<td>O$_3$ (+M) $\rightarrow$ O + (+M)</td>
<td></td>
</tr>
<tr>
<td>plasma chemistry</td>
<td>$O_2 + O + M \rightarrow O_3 + M$</td>
<td>Electron impact ionization</td>
<td>does NOT contribute to radical production</td>
</tr>
<tr>
<td>• Spatially uniform</td>
<td>HO$_2$</td>
<td>O$_2$ $+$ HO$_2$ $\rightarrow$ O$_2$ + OH/H$_2$O</td>
<td></td>
</tr>
<tr>
<td>• Gradient ↑</td>
<td>H</td>
<td>Increase by a factor of ~6</td>
<td></td>
</tr>
<tr>
<td></td>
<td>OH</td>
<td>Increase by a factor of ~4</td>
<td></td>
</tr>
<tr>
<td>Direct gas heating</td>
<td>A significant portion of plasma enhancement</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Enhancement for T</td>
<td>Increase by ~20%; gradient ↑</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

![Figure 11](image.png)

Figure 11. Spatial distributions of (a) $E/N$ and electron number density, and (b) measured and predicted OH concentration (squares) and gas temperature (triangles) (red: without plasma; blue: with plasma), at 25 Torr in a H$_2$/O$_2$/N$_2$ flame (equivalence ratio = 0.5) [28]. Reprinted from [28], Copyright 2015, with permission from Elsevier.
in figure 11(b), gradients of radical concentrations and gas temperature are also substantially higher. Both species and gas temperature profiles shift upstream toward the burner (approximately 0.2 cm) at low plasma power, suggesting that plasma accelerates auto-ignition in the pre-heat zone. Joule heating alone could not move the gas temperature and species profiles as far upstream as the pulsed plasma source of the same total power. Closer to the burner, the low gas temperature enhances the formation of O3 and HO2 via three-body recombination from O and H radicals, respectively. O3 travels a short distance downstream until its decomposition when the gas temperature rises to ~500 K. HO2 persists for a longer distance downstream until its decomposition when the gas temperature increases to above ~700 K.

In summary, non-equilibrium chemistry effects are of critical importance in the lower-temperature regions upstream of the flame.

In this configuration, only ~10% of the total input energy is coupled in the pre-heat and reaction zones, while ~90% of the total input energy is coupled in the post-flame zone, which does not enhance the pre-heat zone. To increase the energy coupled in the pre-heat zone, it has been proposed that the high-voltage electrode should be placed closer to the flame, which will require that the material to tolerate higher temperatures.

4.3.2. Non-premixed (diffusion) flame. In this study, a counter-flow diffusion flame is employed at pressures ranging from 60 to 300 Torr, with the oxidizer stream enhanced by plasma discharges. As shown in figure 1(c), this configuration can be divided into four zones: the plasma discharge zone inside the oxidizer tube, the region near the oxidizer tube exit, the radical production zone between the oxidizer tube exit and the flame, and the flame zone. Based on this analysis, a general theory for a plasma-assisted non-premixed (diffusion) flame is developed, and summarized in table 4.

In the radical production zone, due to the higher gas temperature, O3 rapidly decomposes to O2 and O radical, and O2 (a1Δ) rapidly quenches to O2. As a result, only O radical can reach the flame to provide enhancement from plasma.

Following this, the OH radical increases by approximately 10 times in the flame zone, primarily through chain branching reactions of O + H2 → OH + H and O + H2O → 2OH. This increase in OH radical, together with the higher oxidizer flow temperature, results in rapid fuel consumption in the flame zone, including breakup, chain branching, and oxidation (OH + H2/CO → H2O/CO2 + H). In addition, the peak flame temperature also rises noticeably with plasma activation.

If the flame location is identified by maximum temperature location, then plasma shifts both the radical production zone and flame location toward the oxidizer tube exit. Plasma also significantly increases the extinction strain rates by more than two times, to sustain stable lean combustion.

5. Conclusions

An integrated theoretical/numerical framework for plasma-assisted ignition and combustion is reviewed. Three physical configurations are considered to cover ignition and premixed and non-premixed flames. A two-temperature model is employed for non-equilibrium plasma. It is found that modeling must be at least 1D to capture cathode sheath formation, and to calculate E/N accurately. The plasma-combustion chemistry mechanisms for a wide range of fuel types are examined to illustrate how to develop such mechanisms from existing air-plasma chemistry and fuel combustion chemistry.

Modeling strategies are explored and summarized. The ‘frozen electric field’ strategy utilizes the quasi-periodic behaviors of the electrical characteristics to avoid re-calculation during each pulse. To deal with the intense calculation of large and stiff chemistry and the evaluation of associated transport properties, a point-implicit stiff ODE solver (ODEPIM) and correlated dynamic adaptive chemistry and transport (CO-DACT) strategy are employed. CO-DACT generates locally reduced kinetics mechanisms for each spatial location and time step. Only the reaction rates of selected species and reactions are calculated, while the rest are frozen to reduce the chemistry calculation. A three-stage multi-time scale modeling strategy takes advantage of the separation of time scales in nanosecond pulsed plasma discharges to dynamically adjust the time step size for simulations.

### Table 4. General theory for plasma-assisted non-premixed (diffusion) flame.

<table>
<thead>
<tr>
<th>Zone</th>
<th>T</th>
<th>Chemistry</th>
</tr>
</thead>
<tbody>
<tr>
<td>Discharge</td>
<td>Initial T</td>
<td>Afterglow: O2 + O + M → O3 + M</td>
</tr>
<tr>
<td>Oxidizer tube exit</td>
<td>Plasma → preheated T</td>
<td>Only long lifetime species survive: O, O3, O2(a1Δ)</td>
</tr>
<tr>
<td>Radical production zone: shift upstream</td>
<td>Preheated T→ flame T</td>
<td>O2 (a1Δ) → O2 + O (a1Δ) rapidly; O2(a1Δ) → O2 rapidly; only O survives</td>
</tr>
<tr>
<td>Flame zone: shift upstream towards the oxidizer tube exit</td>
<td>Flame T (dominant)</td>
<td>O enhances chain branching: O + H2 → OH + H; O + H2O → 2OH ⇒ OH† ~ 10 times (larger at low p)</td>
</tr>
</tbody>
</table>

⇒ rapid fuel consumption: breakup, chain branching, oxidation (OH + H2/CO → H2O/CO2 + H)
A general theory of plasma-assisted ignition and combustion is developed. The theory has three major components: a multi-time scale theory for nanosecond pulsed plasma discharges, a theory for plasma-assisted ignition, and theories for plasma-assisted premixed and non-premixed flames.

A multi-time scale theory for nanosecond pulsed plasma discharge sets the foundation of plasma enhancement for ignition and combustion; it can be divided into four stages based on the time scales of the underlying physical processes. Stage I is the discharge pulse, which has time scales of O (1–10 ns). In this stage, most input energy is coupled into electron impact excitation and dissociation reactions, to generate a large amount of excited species and radicals under low gas temperatures. Stage II is the afterglow phase during the gap between two adjacent pulses, and has time scales of O (100 ns). Quenching of excited species is the primary physical process in this stage. It not only further dissociates both O₂ and fuel molecules to generate radicals under low gas temperatures, but also provides fast gas heating. Stage III is the remainder of the gap between two adjacent pulses, with time scales of O (1–100 μs). The radicals generated during Stages I and II significantly enhance the exothermic chain propagation and termination reactions in this stage. Stage IV takes place after a large number of pulses, with time scales of O (1–1000 ms). This stage includes weak and slow reactions, convective and diffusion transport, and the cumulative effects of multiple pulses, including preheated gas temperatures and a large pool of radicals and fuel fragments.

Plasma-assisted ignition can be divided into three stages: the first stage ignition to ‘cool flame’ (only for fuels with LTC), the second stage ignition to hot flame, and the ignition kernel propagation. In the first stage, plasma generates a large amount of e, O (³D), O, H, and OH, enhancing the H-abstraction of fuel molecules, which in turn either significantly enhances (below ~700–800K) or re-activates (above ~700–800 K) the exothermic LTC chain branching positive feedback cycle. In the second stage, the radicals from the first stage trigger and enhance the exothermic high gas temperature chain branching cycle, which leads to ignition of hot flames. The acceleration of ignition is a function of input energy. The ignition kernel propagation is close to auto-ignition triggered by radicals and pre-heating at different locations; it is much faster than laminar flame speed and requires lower input energy than purely thermal ignition.

For premixed and non-premixed flames, plasma could significantly enhance the radical generation and gas heating in the pre-heat zone, thereby leading to ultra-fast auto-ignition and/or flashback.

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